

Summary of design process

AE 353

Spring 2023

Bretl

$$\dot{m} = f(m, n)$$

↓

$$0 = f(m_e, n_e)$$

↓

$$\dot{x} = Ax + Bu$$

← $x = m - m_e \quad u = n - n_e$

$$A = \left. \frac{\partial f}{\partial m} \right|_{m_e, n_e} \quad B = \left. \frac{\partial f}{\partial n} \right|_{m_e, n_e}$$

$$u = -Kx$$

↓

$$\dot{x} = (A - BK)x$$

↓

$$x(t) = e^{(A - BK)t} x(0)$$

→

asymptotically stable

↓

$$x(t) \rightarrow 0 \text{ as } t \rightarrow \infty$$

↑

this is true if and only if all eigenvalues of $A - BK$ have negative real part